

Massive-material-injection-triggered disruptions



DE LA RECHERCHE À L'INDUSTRIE

**What do we understand?
What is still unclear?**

E. Nardon, F.J. Artola, D. Bonfiglio, M. Hoelzl, D. Hu, M. Kong,
S.J. Lee, M. Lehnen, A. Matsuyama, S. Sadouni, K. Särkimäki,
C. Sommariva, F. Wieschollek

Runaway Electron Meeting, Garching, May 2022

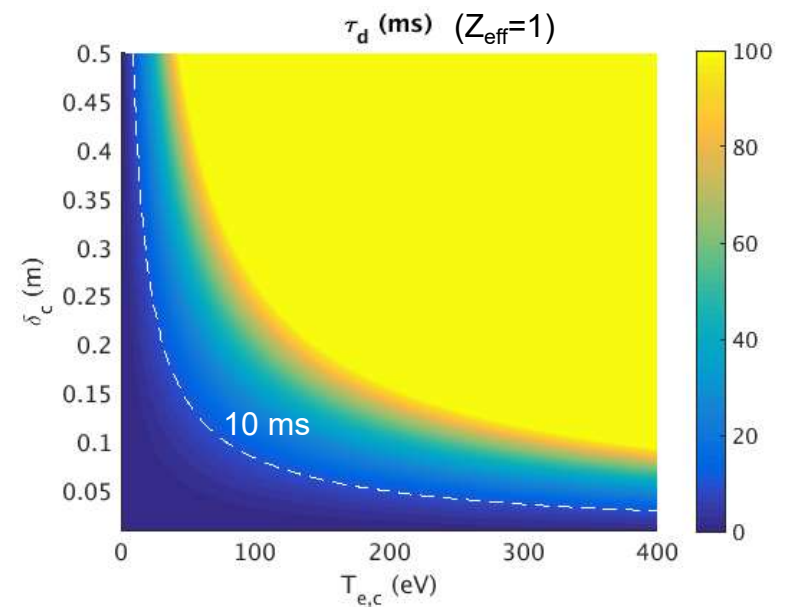
- Presentation not focused on specific recent work

- Instead, will try to summarize current understanding, speculations and questions about Massive Material Injection (MMI) -triggered disruptions
 - MMI = Massive Gas Injection (MGI) or Shattered Pellet Injection (SPI)
 - Based mainly on JOEUK and INDEX simulations
 - Focus on the pre-Thermal Quench (TQ) and TQ phases

- What is the Thermal Quench (TQ)?
- TQ triggering mechanisms
 - The importance of a cold front
 - To have or not to have a cold front
 - Importance of non-axisymmetry
 - Characteristic // transport scales and T_e holes
 - The role of helical cooling
- TQ dynamics: difference between large and small I_p spike
- Field line stochasticity and implications for RE generation

- As the name says, the TQ is a loss of thermal energy. OK, but...
- The TQ is typically associated to strong **MHD activity** and an I_p spike
- Nature of the MHD activity?
 - **2/1 tearing mode** seems key in most cases [[de Vries et al. NF 2016](#), [Nardon et al. PPCF 2021](#), ...]
 - 1/1 internal kink mode may participate, but probably does not suffice alone
 - Justification: 1/1 crash will not produce I_p spike unless edge plasma is very cold (think of sawteeth)... But if edge plasma is very cold, 2/1 TM should be present too
- A **radiative collapse** throughout the plasma is needed for a full TQ
 - Heat diffusion along stochastic FLs not efficient below ~ 100 eV [[Ward & Wesson NF 1992](#)]
 - Need **impurity influx** and **mixing**
 - Full TQ often not obtained in 3D non-linear MHD sims.!
 - Probably related to impurities, but difficult to investigate because of numerical issues

- A cold front causes a **current profile contraction** and thereby **drives MHD** (in part. the 2/1 TM)
- What do we mean by 'cold'?
- Resistive current decay time in region of perp. size δ_c and resistivity η_c : $\tau_d = \mu_0 \delta_c^2 / \eta_c$
 - Spitzer resistivity: $\eta_c = 2.8 \cdot 10^{-8} \cdot Z_{\text{eff}} / T_{e,c} [\text{keV}]^{3/2}$
- τ_d can be compared to several things, e.g.:
 - For SPI, $\tau_{\text{shards} \rightarrow \text{core}}$
 - $\tau_{\text{disruption warning}}$
- We choose to compare τ_d to 10 ms to fix ideas
 - For τ_d to be < 10 ms, one needs $T_{e,c} < 30 \text{ eV}$ when $\delta_c = 0.2 \text{ m}$
- Note that critical $T_{e,c}$ scales like $\delta_c^{-4/3}$!



[Nardon et al. NF 2020]

- JOREK SPI simulations sometimes produce a cold front, sometimes not...
- Reasons are under investigation
- $T_{sim.} \sim T_{shards \rightarrow core}$ probably plays a key role

All for pure Ne or mixed Ne+D₂ SPI

Machine / Scenario	Author of sims.	Cold front?	R(m) / a(m)	Pellet velocity (m/s)	$T_{shards \rightarrow core}$ ($\sim T_{sim}$) (ms)	$\langle n_{Ne} \rangle$ when shards reach the core ($10^{19}m^{-3}$)
ITER Hyd. L-mode	Di Hu	Marginal	6.2 / 2	500	4.0	1.0
JET H-mode	Daniele Bonfiglio	Yes	2.96 / 1.25	200	$\sim 10^*$	2.1
KSTAR H-mode	Sang-Jun Lee	No	1.8 / 0.5	400	1.2	2.0

*Shards path does not quite pass through plasma center

- Simple considerations help interpret results from previous slide...
- Idealized picture: **SPI = 2 step process**
 - 1) Ablation and dilution cooling
 - 2) Radiative Collapse (RC)
- 2 steps because **ablation rate** $\sim T_e^{5/3}$ \rightarrow Drops strongly as T_e drops
- Self-reg. via abl. rate $\rightarrow T_e$ 'always' \sim **a few 100 eV** after 1st phase
 \rightarrow Generating a cold front with SPI **requires RC**
 (origin of the idea of pure D₂ SPI [Nardon et al. NF 2020])
- Time it takes for RC to occur (very simple model – isolated system):

$$\tau_{RC} \sim eT_e n_e / P_{rad} \sim eT_e / (L_{rad} n_{imp})$$

Assuming $L_{rad} \sim 10^{-33} \text{ W.m}^3$ and $T_{e, \text{post-1st phase}} \sim 400 \text{ eV}$, one gets:

$$\tau_{RC} \sim 6 \times 10^{16} / n_{imp}$$

\rightarrow E.g. for $n_{imp} = 2 \times 10^{19} \text{ m}^{-3}$, $\tau_{RC} \sim 3 \text{ ms}$

Radiative cooling rate (L_{rad})
at coronal equilibrium

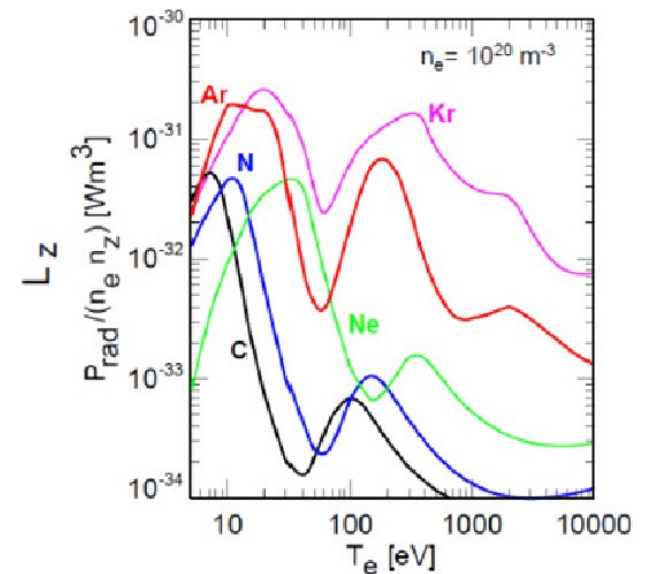
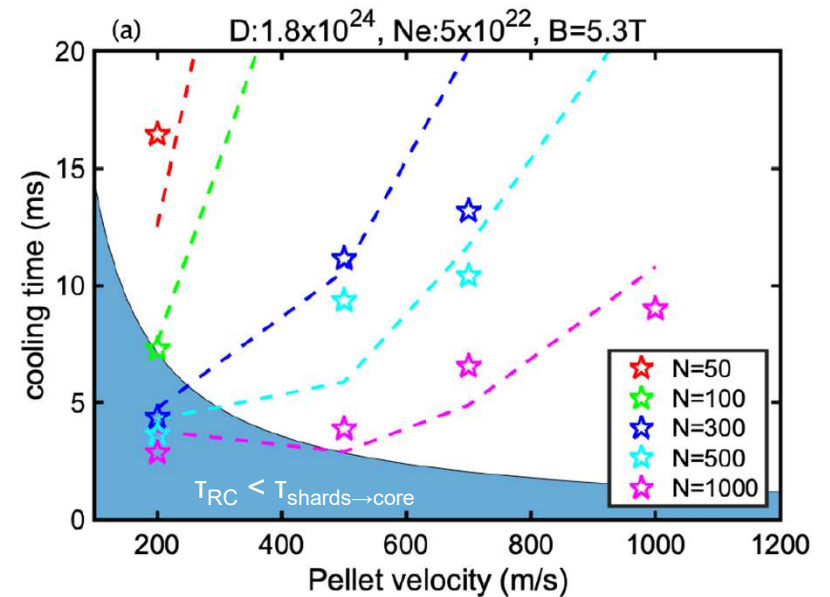


Fig. from
https://www.researchgate.net/figure/Co-oling-rate-Lz-as-sum-of-bremmstrahlung-recombination-and-line-radiation-from-ADAS-for_fig1_315457459

- INDEX 1.5D transport modelling and simple 0D model show that T_{RC} can be $<$ or $>$ $T_{shards \rightarrow core}$ depending on pellet velocity, shard size, etc.
- Suggests possibility of diluting the plasma before triggering the TQ
- But these are axisymmetric results...



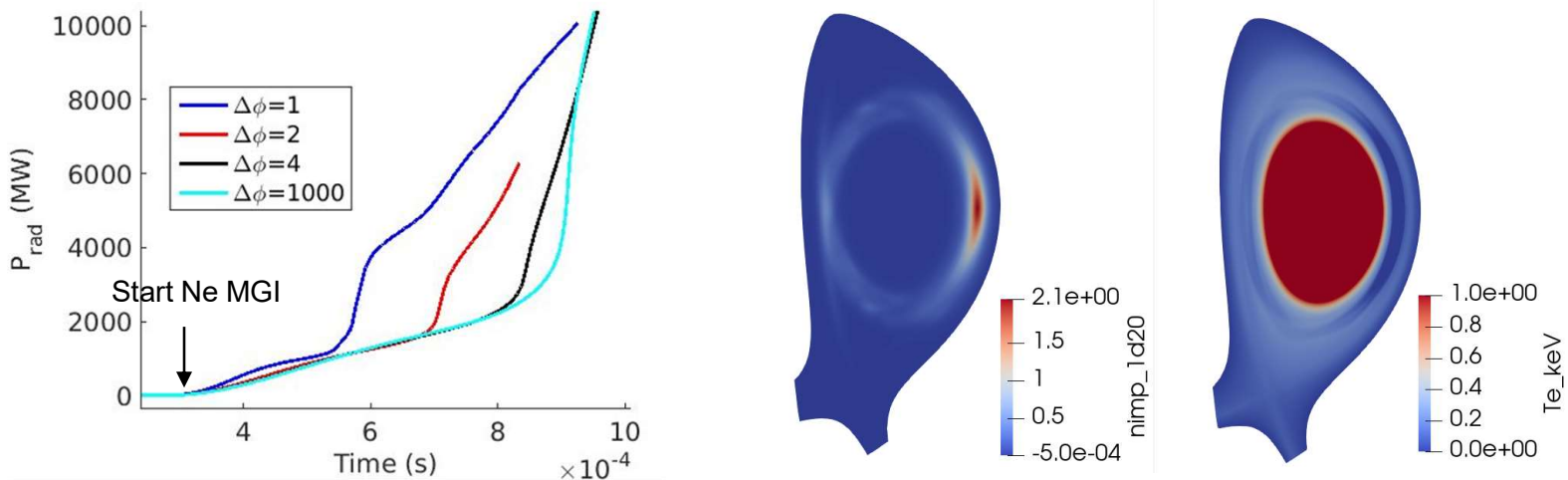
Stars = INDEX sims.; Dashed lines = 0D model

[Matsuyama et al., to be submitted]

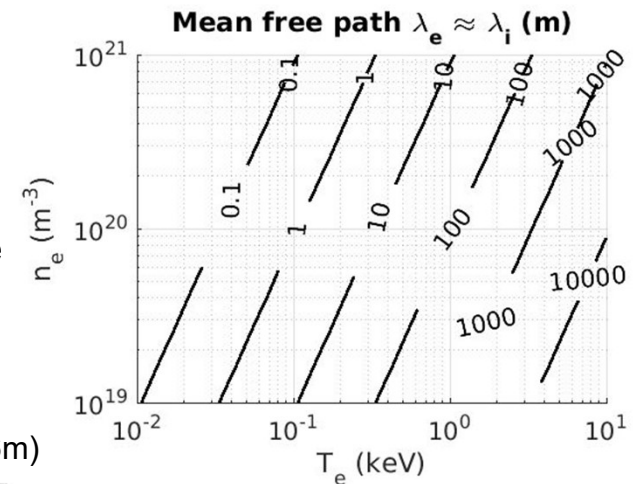
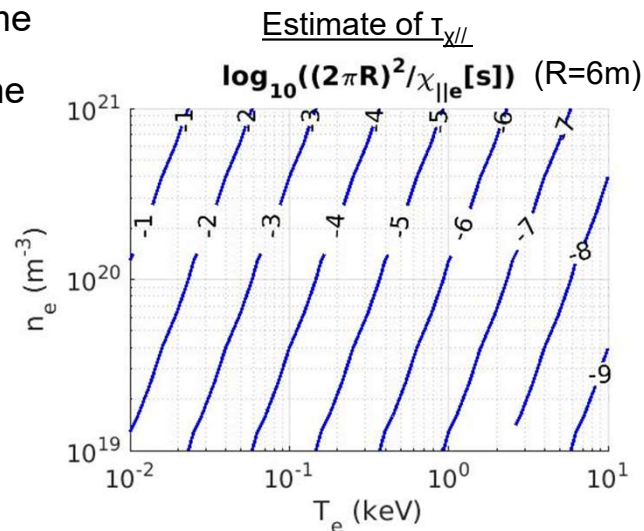
Importance of non-axisymmetry: effect of ablation plasmoid spatial extent

- $(P_{\text{rad}})_{\text{plasmoid}} \sim \int n_e n_{\text{imp}} dV \sim \int n_{\text{imp}}^2 dV \sim N_{\text{imp}}^2 / V_{\text{plasmoid}}$
 - Assumptions: electrons mainly come from impurities; L_{rad} independent of T_e
- Radiative Collapse (RC) easier for smaller V_{plasmoid}
- In JOEUK & INDEX simulations, V_{plasmoid} is usually **largely exaggerated** → RC much harder than in reality!

JOEUK sims. of Ne MGI in ITER: scan in toroidal extent of Ne source $\Delta\Phi$

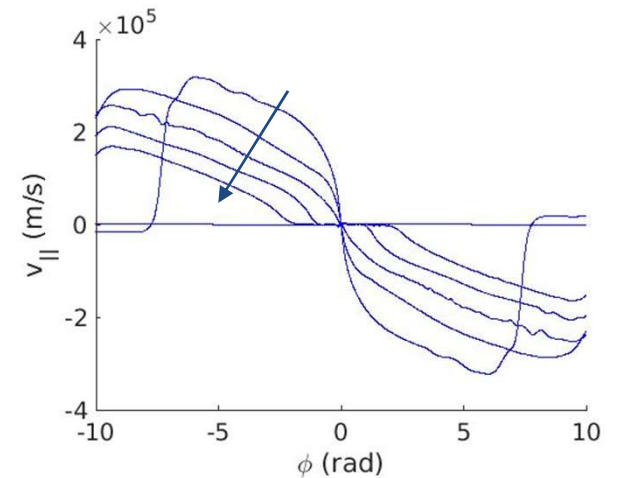
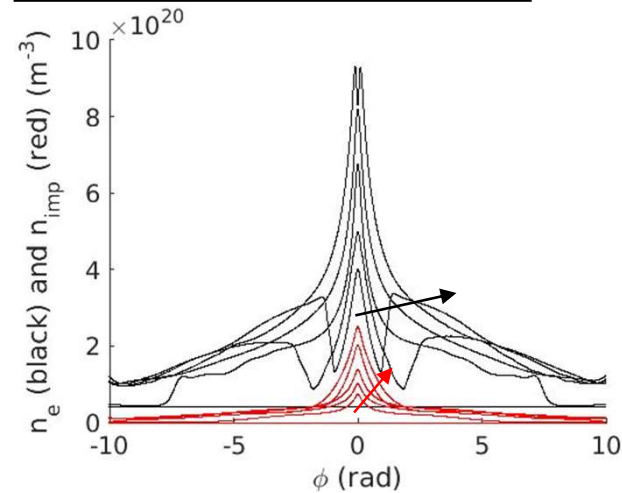
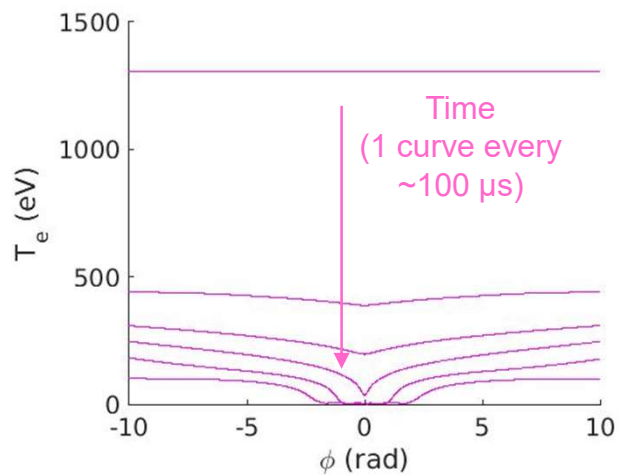


- Typically, length of plasmoid's flux tube $L_{//} \sim 4\pi^2 aR/r_{\text{plasmoid}} \gg 2\pi R$
- Below a certain T_e , $\lambda_e \ll L_{//} \rightarrow //$ heat transport is diffusive
 - $\lambda_e \equiv$ electron mean free path
 - Transition to **diffusive regime** happens before radiative collapse
- Below a certain T_e , $\tau_{X//} > \tau_{RC} \rightarrow$ Expect T_e hole
 - $\tau_{X//} \equiv //$ thermal diffusion time
 - $\tau_{RC} \equiv$ radiative collapse time



- As expected, T_e holes appear in JOREK simulations

JOREK sim. of Ne MGI in ITER



- Should probably think of SPI as creating many T_e holes (which merge?)
- Consequences on P_{rad} and its asymmetry, on MHD?
- Consequences of JOREK lacking resolution to get realistic plasmoids & T_e holes?

- Magnetic island = quasi-isolated helical flux tube
- A thermal instability (collapse) can develop there [Rebut and Hugon, IAEA 1984]: 'radiative tearing mode'

Resistivity $\uparrow\uparrow \rightarrow$ Current decays inside the island \rightarrow Island grows further (like for NTMs)

- Potential effect can be roughly estimated, assuming all current initially inside island is removed

- Method:

1) Estimate δI from j_0 and island width w : $\delta I \approx j_0 \pi a w / m$

2) Estimate δB_r from δI (Biot and Savart): $\delta B_r \approx \mu_0 m \delta I / (2\pi^2 a) \approx \mu_0 j_0 w / (2\pi)$

3) Use w from island theory ($\sim \delta B_r^{1/2}$)

4) Solve for w

$$w = 4 \left(\frac{r q \hat{B}_r}{m q' B_\theta} \right)_s^{1/2} \quad [\text{Wesson, Tokamaks}]$$

- Crude estimate:

$$q/q' \approx a; \quad r \approx a; \quad B_\theta \approx B/10$$

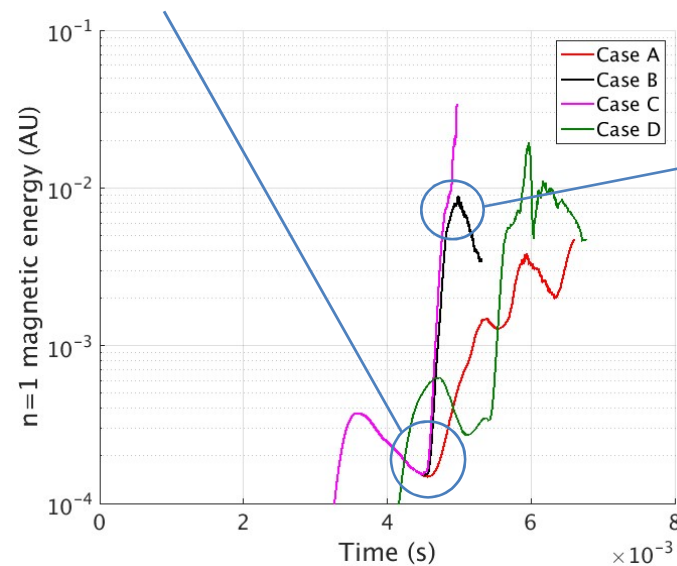
$$\rightarrow w \approx 10a(\delta B_r / (\text{mB}))^{1/2} \rightarrow w \approx 2 \cdot 10^{-5} a^2 j_0 / B \approx 5 I_p [\text{MA}] / B \rightarrow \text{Huge!}$$

\rightarrow This is a potentially very strong mechanism!

- Numerical experiments based on an Ar MGI case in JET

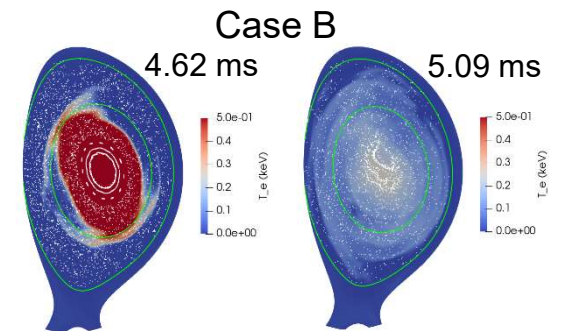
Cases B and C diverge from A as we move the Ar source into the 2/1 island to promote thermal drive

[Nardon et al. PPCF 2021]



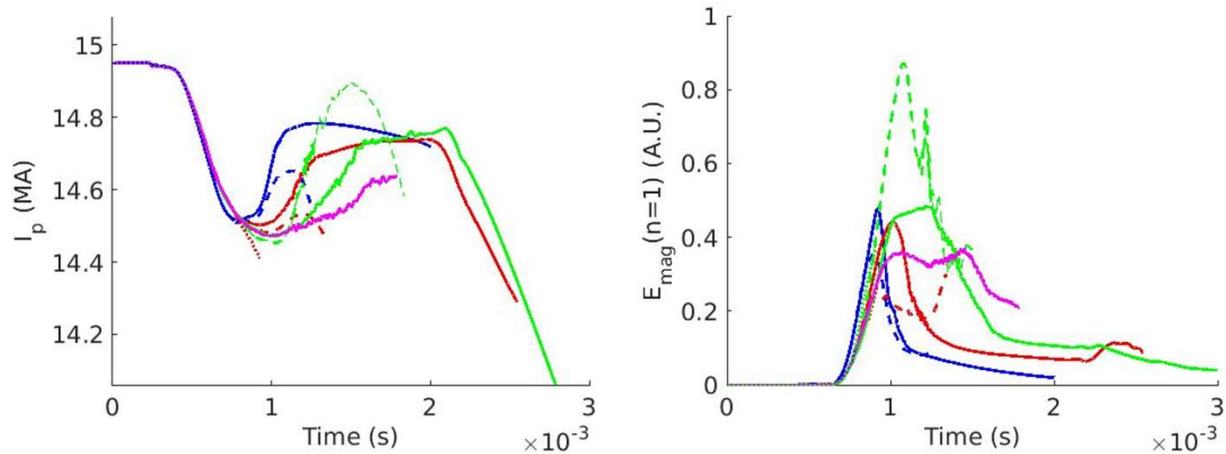
Cases B and C diverge from each other later on because of larger Ar source in C → Stronger thermal drive

- Note: at some point, magnetic stochasticity appears → Heat arrives and 'fights' thermal drive



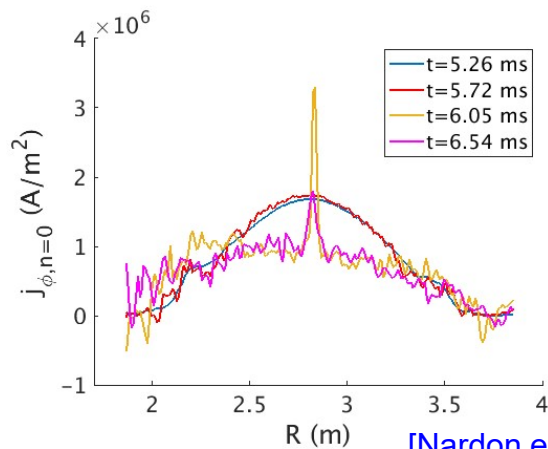
- It is relatively 'easy' to get a small I_p spike with JOREK
 - Correlated with $n=1$ (probably 2/1) mode amplitude

JOREK sims. of MGI in ITER (done for 'academic' purposes)

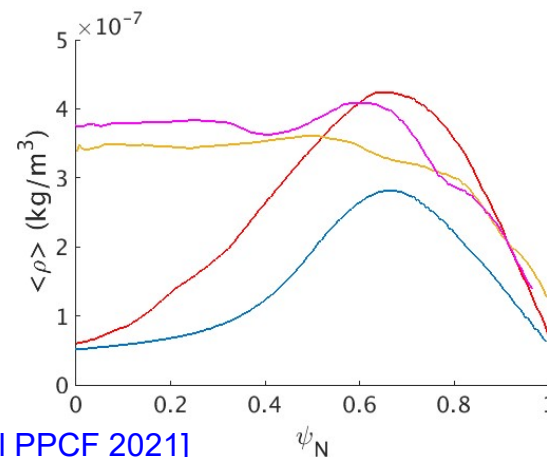


- It is much harder to get a large (realistic*) I_p spike due to numerical issues
 - *Not all experimental disruptions have a large I_p spike
- JOREK sims. with large I_p spike have a distinct strong macroscopic flow in the core (even w/o 1/1 mode)
 - Mixes poloidal flux \rightarrow flattens $j_{||}/B$ and gives the large I_p spike
 - Mixes particles & impurities
- Needs investigations!

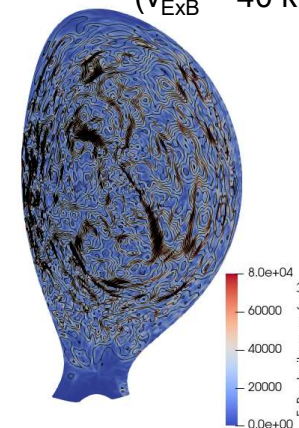
JOREK sim. of Ar MGI in JET with large realistic I_p spike



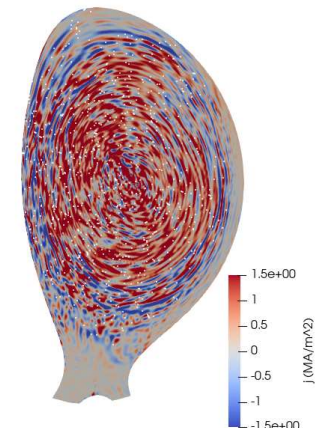
[Nardon et al PPCF 2021]



ExB streamlines
($v_{EXB} \sim 40$ km/s)

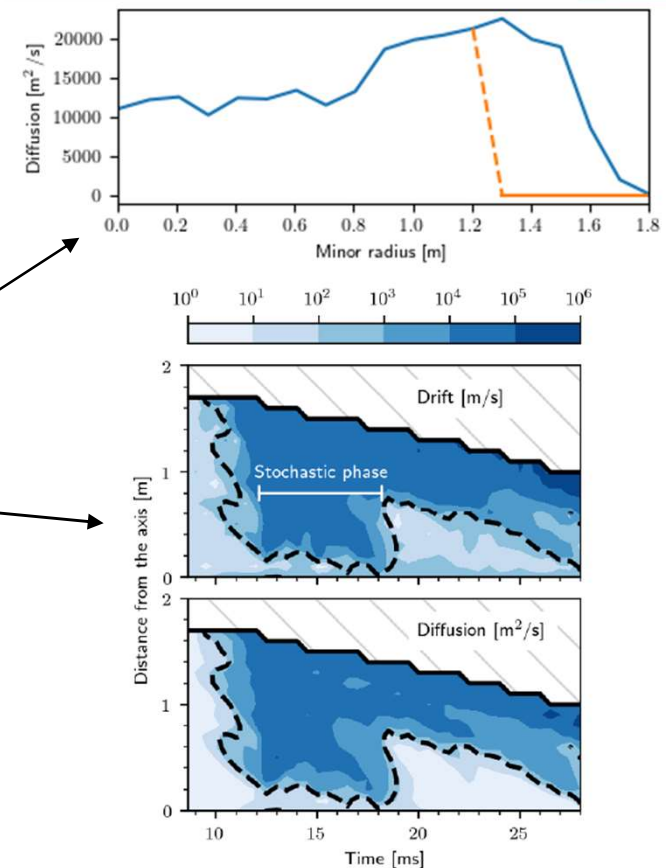


j_ϕ



- Stochastic transport is **not just 'on' or 'off'**
- Konsta Särkimäki calculates advection and diffusion coefficients by post-processing JOREK sims. with test electrons – see his talk on Wednesday!
- Edge Transport Barrier (ETB) found in ITER SPI sim. by Di Hu with marginal cold front (no large 2/1 mode)
- No ETB in a cold VDE simulation which starts with a large MHD crash including large 2/1 tearing mode [\[Artola NF 2022\]](#)

→ Missing the cold front probably has important consequences on predicted stochastic losses (among other things)



[Särkimäki, submitted, <https://arxiv.org/abs/2203.09344>]

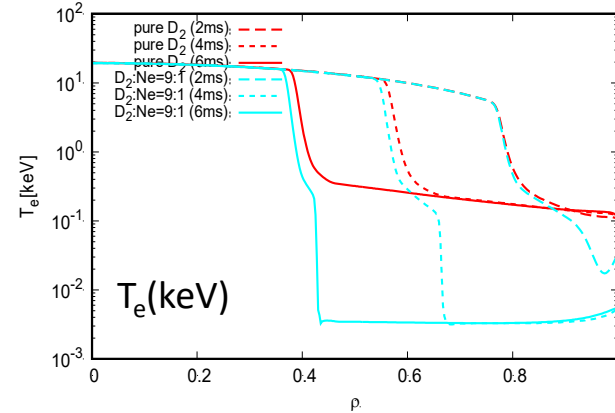
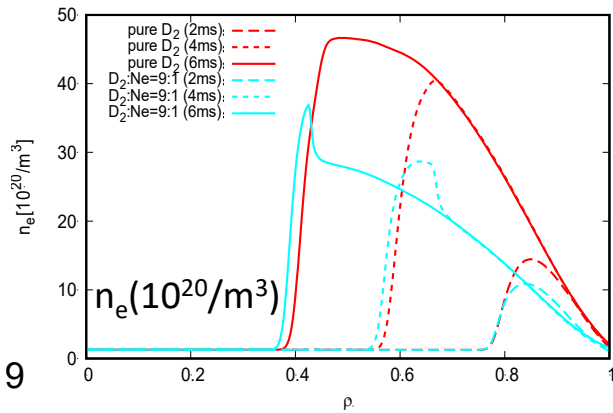
- Generation of **cold front** and **helical cooling** probably key to TQ trigger and dynamics
 - These depend on **energetics** of plasmoids and their environment (question of the **radiative collapse**)...
 - ...Which depends on the **spatial extent** of the plasmoids
- Should be investigated and consequences for JOEAK modelling with over-sized plasmoids drawn
- Practical question for ITER DMS: **is it possible to dilute the whole plasma before triggering a TQ?**
 - Pure H₂ SPI would seem ideal but suffers from plasmoid drifts → Poor fueling efficiency
 - What about $\epsilon\text{Ne}+(1-\epsilon)\text{H}_2$?
 - Or maybe still pure H₂, but lots of it?
 - **Physics of the TQ** has to be clarified
 - Numerical issues still a bottleneck to study cases with a large I_p spike

Backup slides

Pure D₂ SPI may be needed to fuel enough before triggering a TQ

ITER baseline 15MA H-mode plasma

Single 28.5mm (L/D=2) pellet, $V_p = 200\text{m/s}$, $N_{\text{shards}} = 300$: pure D₂ vs. D₂:Ne=9:1



INDEX sims.

A. Mastuyama, 2019

With Ne+D₂ SPI:

Radiative collapse in cold front

- ⇒ T_e goes down to a few eV
- ⇒ Resistive j decay time $< a/V_p$
- ⇒ Modification of j profile
- ⇒ TQ triggering when cold front reaches $q=2$

